



Fermilab

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Magnetic Design of Small-Aperture Dipoles of the Shell and Block Type

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Abstract:

This note collects viewgraphs from a talk presented at the workshop "Magnets for a Very Large Hadron Collider" held at Port Jefferson in November 1998. The workshop was organized by the Magnet Technologies Working Group, appointed by the Steering Committee for a Very Large Hadron Collider. Goal of the workshop was to develop innovative concepts in magnet design and fabrication, that would result in significant cost reductions. In particular, the present study is devoted at exploring the magnetic performance of small-aperture dipoles. After some general considerations on the choice of the optimal design field as function of aperture and conductor parameters, two designs are presented, one of the shell type and one of the block type. In both cases, the design parameters are 30 mm aperture and 12-13 T short sample field (assuming a current density of 2-3 kA/mm² at 12 T and 4.2 K). The two designs are compared between them and with a 50 mm aperture design of comparable performance, which is being developed by a collaboration involving Fermilab, LBL and KEK. It is found that, for these parameters, the 30 mm aperture magnet allows substantial savings in superconductor with respect to the 50 mm case, and that the shell and block designs are substantially equivalent in terms of conductor efficiency and field quality. A comparison of vertical vs. horizontal layout of the two apertures in a two-in-one magnet of the block type is also carried out. It is found that the vertical layout, which present interesting features from the fabrication standpoint, requires substantially larger yoke in order to achieve the same transfer function.

Magnetic design of small-aperture dipoles of the shell and block type



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- Choice of design parameters
- Shell vs. Block type design:
 - conductor efficiency
 - field quality
- Two-in-one: yoke diameter requirement for horizontal vs. vertical layout
- Conclusions

Aperture requirement



SSC: 40 → 50 mm LHC: 50 → 56 mm

VLHC: 50 → 30 mm?

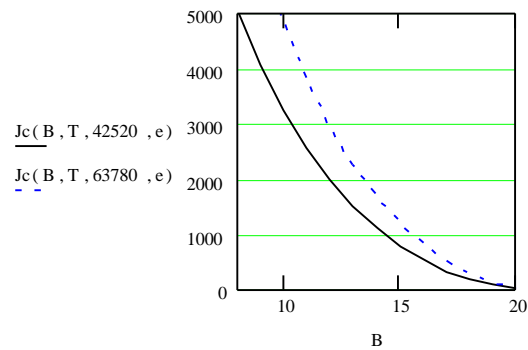
Charge: Guided by the snowmass '96 parameter set, explore and develop innovative concepts that will result in significant cost reductions.

Critical current density



$$J_c(B, T, C0, e) := \frac{C(C0, e)}{\sqrt{B}} \cdot \left(1 - \frac{B}{Bc2(T, e)}\right)^2 \cdot \left[1 - \left(\frac{T}{Tc0(e)}\right)^2\right]^2 \quad (\text{Summers, L, IEEE Trans. Mag 27-2})$$

$$J_c(12T, 4.2K) = 2 - 3 \text{ kA}$$

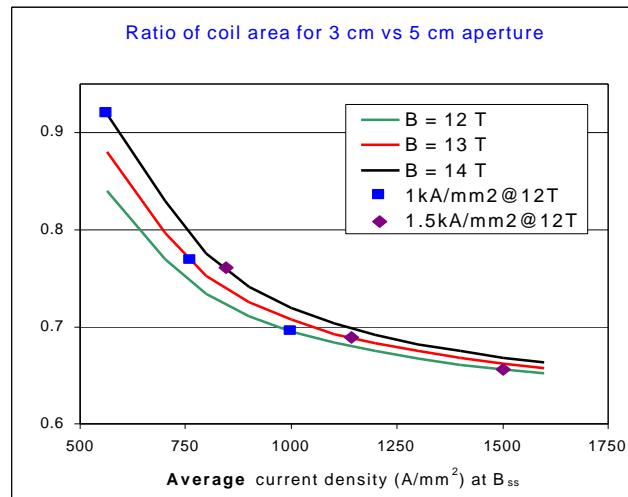


Magnets for a Very Large Hadron Collider
Port Jefferson, November 16-18, 1998

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Choice of design parameters: conductor efficiency

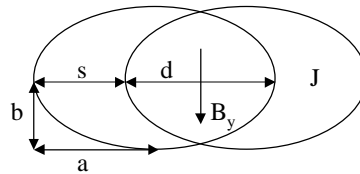


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Based on intersecting ellipses model



$$B_y = -\frac{\mu_0 J s b}{a + b}$$

$$s(J, d, B) := \frac{-2 \cdot d \cdot B}{B + \mu_0 J \cdot d}$$

$$a(J, d, B) := \frac{s(J, d, B) + d}{2}$$

$$b(J, d, B) := \frac{d}{2} \cdot 1.1$$

$$A_{oq}(J, d, B) := a(J, d, B) \cdot b(J, d, B) \cdot \left(\frac{\pi}{4} - \frac{1}{2} \cdot \frac{s(J, d, B)}{a(J, d, B)} \cdot \sqrt{1 - \frac{s(J, d, B)^2}{4 \cdot a(J, d, B)^2}} - \frac{1}{2} \cdot \arcsin \left(\frac{s(J, d, B)}{2 \cdot a(J, d, B)} \right) \right)$$

$$A_{hc}(J, d, B) := \frac{\pi \cdot a(J, d, B) \cdot b(J, d, B) - A_{oq}(J, d, B)}{2}$$

Design parameters



Coil aperture	:	30 mm
Coil width	:	27 mm
Coil layout	:	shell/block
No. of layers	:	3
Maximum field	:	12 T ($J_c(12T, 4.2K)=2 \text{ kA/mm}^2$)
	:	13 T ($J_c(12T, 4.2K)=3 \text{ kA/mm}^2$)
Geom. Harmonics	:	$< 10^{-4}$ @ 1cm
Stress (Lorentz)	:	$< 100 \text{ MPa}$

Shell type design: cable parameters



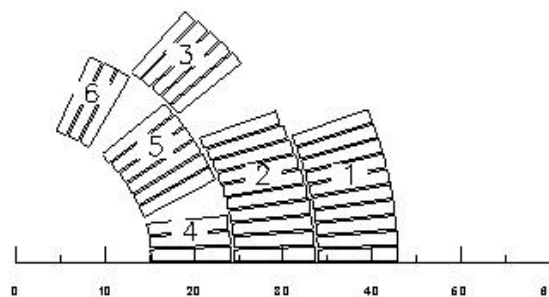
Strand diameter	mm	0.75
Cu/Sc ratio		1:1
No. of strands		24
Area of superconductor	mm ²	5.301
Cable width (bare)	mm	9.0
Cable mid-thickness (bare)	mm	1.35
Keystone angle	deg	1.8
Transposition length	mm	120
Compaction (area)	%	88.3
Compaction (inner edge)	%	80
Compaction (outer edge)	%	100
Radial insulation	mm	0.150
Azimuthal insulation	mm	0.120

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Shell-type design: coil cross-section



- 3 layer, 6 block design

- Optimized with ROXIE

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Block type design: cable parameters



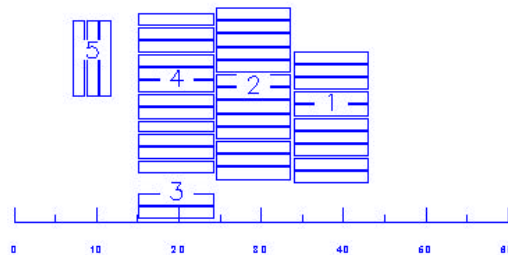
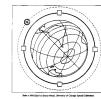
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No. of strands		24
Area of superconductor	mm ²	5.301
Cable width (bare)	mm	9.0
Cable mid-thickness (bare)	mm	1.35
Keystone angle	deg	0.0
Transposition length	mm	120
Compaction (area)	%	88.3
Compaction (inner edge)	%	90
Compaction (outer edge)	%	90
Radial insulation	mm	0.150
Azimuthal insulation	mm	0.120

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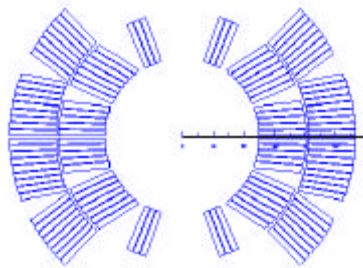
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50 mm bore, 2 layer shell type dipole design



- FNAL/LBL/KEK collaboration
- Cross section from FNAL TD-98-039
- Optimization work still underway (last update Oct 30)



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Short sample performance/conductor efficiency



Parameter	Unit	Shell	Block	50 mm
SC area (1 quadrant)	mm ²	196	212	398
$J_c(12T, 4.2K) = 2 \text{ kA/mm}^2$				
I_{ss}	kA	10.1	10.1	18.0
$B_{ss}^{(0)}$	T	11.9	12.0	12.9
$B^{(max)}$ (layer 1)	T	12.2	12.2	13.2
$B^{(max)}$ (layer 3)	T	6.2	5.3	
$J_c(12T, 4.2K) = 3 \text{ kA/mm}^2$				
I_{ss}	kA	11.0	11.1	19.4
$B_{ss}^{(0)}$	T	13.0	13.1	13.9
$B^{(max)}$ (layer 1)	T	13.3	13.3	14.2
$B^{(max)}$ (layer 3)	T	6.8	5.8	

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Energy and forces



Parameter	Unit	Shell	Block	50 mm
Operating current	kA	10.2	10.1	16.7
Stored energy	MJ/m	0.35	0.41	0.73
Inductance	mH/m	6.7	8.0	5.2
$-\Sigma F_y$ (1 quadrant)	MN/m	0.9	0.8	1.2
ΣF_x (1 quadrant)	MN/m	2.0	2.3	3.1
Stress (Φ/y , 1 st layer)	MPa	86	28	100
Stress (Φ/y , 2 nd layer)	MPa	84	36	75

Geometric harmonics



10^{-4} @ 1cm

Component	Shell	Block	50 mm
b_3	0.1	-0.1	0.0
b_5	0.3	0.3	-0.1
b_7	0.7	0.6	0.0
b_9	0.6	-0.8	0.1
b_{11}	2.9	1.2	0.0
b_{13}	-0.5	0.2	0.0

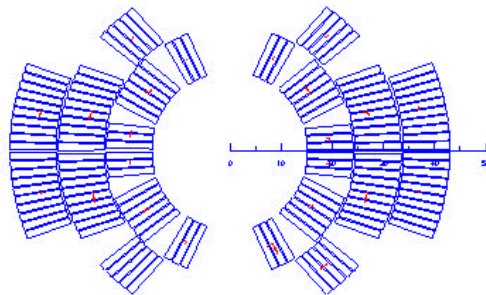
Random errors



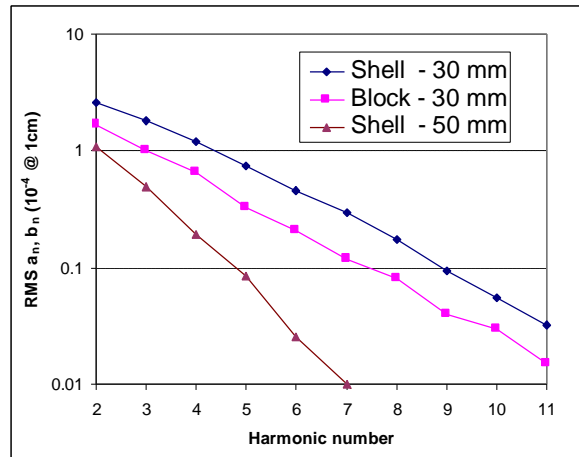
Random block displacement simulation using ROXIE

Shell: $\pm 50 \mu\text{m}$ radial/azimuthal displacements

Block: $\pm 50 \mu\text{m}$ horizontal/vertical displacements



Random errors



- No longitudinal averaging

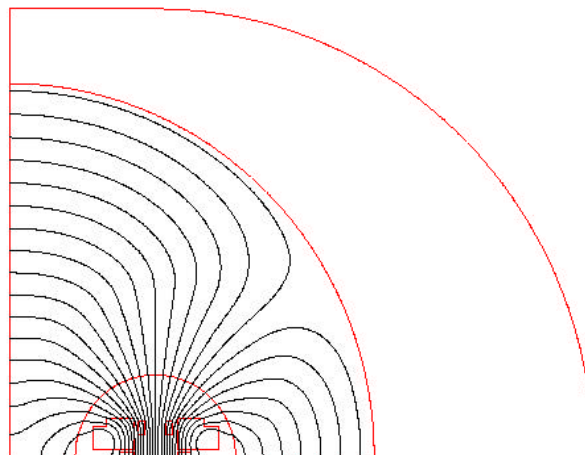
- Magnetic measurements?

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Horizontal two-in-one layout

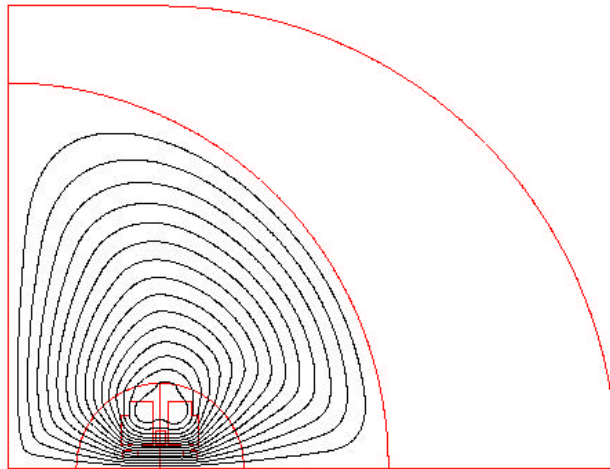


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Vertical two-in-one layout

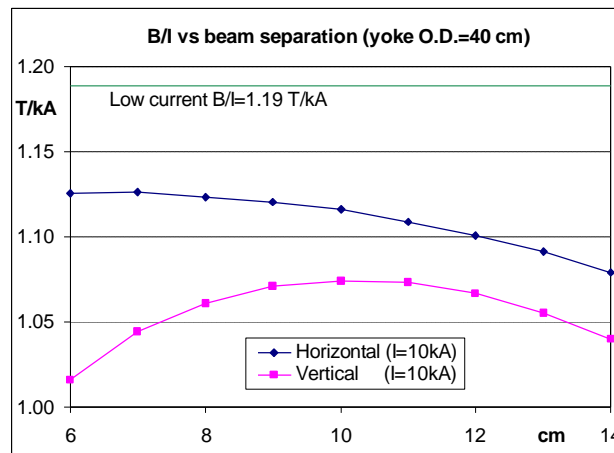


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Transfer function for 40 cm yoke diameter

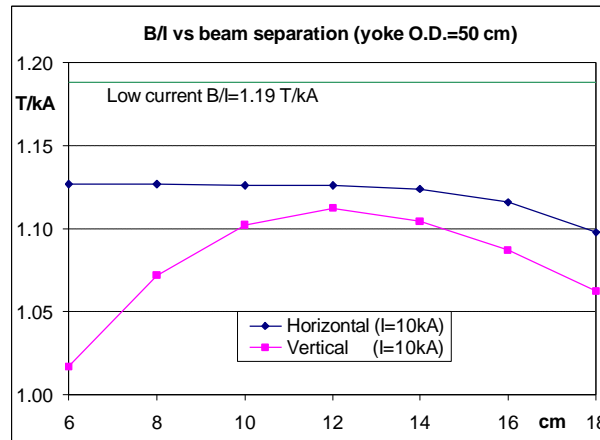
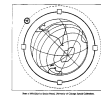


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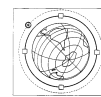
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Transfer function for 50 cm yoke diameter

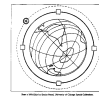


Next steps



- Field quality: further optimize geometric harmonics, evaluate magnetic measurement accuracy.
- End field quality (in particular for block type design).
- Mechanical parameters for conductor groups in the end regions (for shell type design).

Conclusions



- 30 mm bore dipole with 12-13 T design field using Nb₃Sn conductor at 4.2 K allows substantial savings in superconductor wrt 50 mm bore magnet with same design parameters.
- For these design parameters, shell and block design are substantially equivalent in terms of conductor efficiency and field quality.
- Vertical arrangement of the two apertures requires 50% larger yoke radius wrt horizontal arrangement in order to achieve same transfer function.